

Ex 12.1.2: a) Applying Dijkstra's algorithm in steps \rightarrow in the following:

Step 1:

Vertex	distance
a	<u>0</u>
b	14
c	∞
f	∞
g	<u>40</u>
h	17
i	∞

Step 2:

a	<u>0</u>
b	<u>13</u>
c	∞
f	∞
g	<u>10</u>
h	16
i	14

Step 3 :

a	0
b	<u>13</u>
c	22
f	23
g	<u>10</u>
h	16
i	<u>14</u>

Step 4 :

a	0
b	<u>13</u>
c	22
f	21
g	<u>10</u>
h	<u>15</u>
i	<u>14</u>

Step 5 :

a	0
b	<u>13</u>
c	22
f	21
g	<u>10</u>
h	<u>15</u>
i	<u>14</u>

Step 6:

a		0
b		<u>13</u>
c		<u>22</u>
f		<u>21</u>
g		<u>10</u>
h		<u>15</u>
i		<u>14</u>

Step 7:

a		0
b		<u>10</u>
c		<u>22</u>
f		<u>21</u>
g		<u>10</u>
h		<u>15</u>
i		<u>14</u>

b) The distances are
a to c: 22
a to f: 21
a to i: 14

Ex 13.1.3 a) We apply the algorithm again:

Step 1:

Vertex	distance
a	0
b	5
c	6
f	∞
g	17
h	∞

Step 2:

a	0
b	5
c	5
f	∞
g	17
h	12

Step 3:

$$\begin{array}{l|l} a & 0 \\ b & 5 \\ c & 6 \\ f & \textcircled{12} \\ g & 17 \\ h & 12 \end{array}$$

Step 4:

$$\begin{array}{l|l} a & 0 \\ b & 5 \\ c & 6 \\ f & 12 \\ g & 16 \\ h & \textcircled{12} \end{array}$$

Step 5:

$$\begin{array}{l|l} a & 0 \\ b & 5 \\ c & 6 \\ f & 12 \\ g & 16 \\ h & 12 \end{array}$$

b) $a-f: 12$, $a-g: 16$
 $a-h: 12$

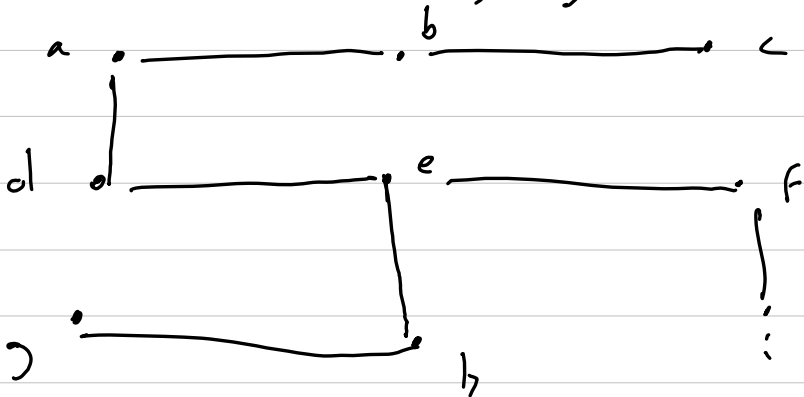
Ex 12.2.1: Kruskal's algorithm:

Add the following edges in order:

1. $e-h$ 2. $a-b$, $b-c$, $d-e$, $e-f$

3. (choices made here) $a-d$

4. (choices) $f-i$, $g-h$.



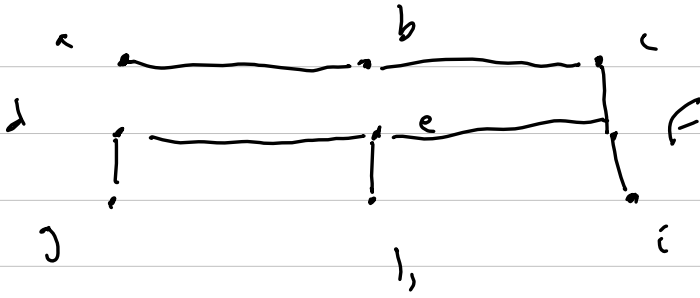
Prim's algorithm:

Step 1: $a-b$, $b-c$

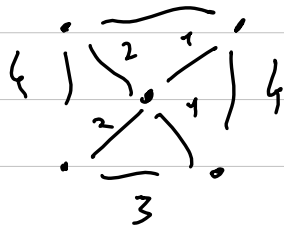
Step 2: (choices) $c-f$

Step 3: $e-f$, $e-h$, $e-d$

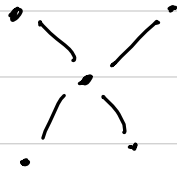
Step 4: (choices) $d-g$, $f-i$



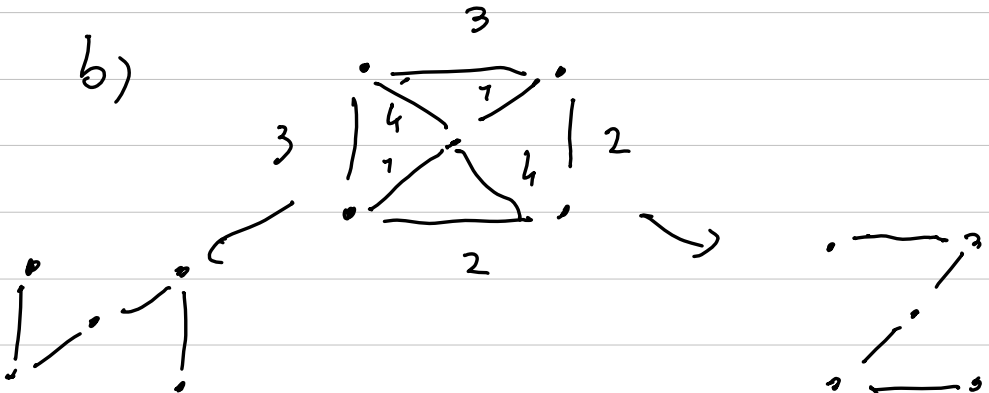
Ex 13.2.2: a) The following assignment



gives a unique minimal tree:



b)



Ex 12.2.4 : We must connect the cities as follows:

G - S - F - S - B - T - E
(initial letters for cities)